# Vapor Pressure and Dissolution Enthalpy Measurements in Ternary $\{H_2O+NaCl+Na_2SO_4\}$ System between 298 K and 363 K

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A nonisothermal static device was used to make measurements of vapor pressures in the ternary {NaCl (1) + Na<sub>2</sub>SO<sub>4</sub> (2) + H<sub>2</sub>O (3)} system between 298 K and 363 K with molality ratios  $m_1/m_2 = 1/10$  and  $m_1/m_2 = 1/1$ . Experimental data were fitted using empirical relation proposed by Appelblat. Dissolution enthalpies of both anhydrous sodium chloride and sodium sulfate in water were also measured up to saturation conditions at 297.8 K, 317.5 K, and 332.4 K (with  $m_1/m_2 = 1/10$ ,  $m_1/m_2 = 1/1$ , and  $m_1/m_2 = 10/1$ , respectively) by using a Setaram C80D differential calorimeter. These calorimetric data were used to establish the analytical expressions of Pitzer and NRTL electrolyte's parameters as a function of temperature. The ability of both models to represent both the dissolution enthalpies and the activities of water were tested.

#### 1. Introduction

Because Na<sup>+</sup>, Cl<sup>-</sup>, and SO<sub>4</sub><sup>2-</sup> are components of natural fluids, a knowledge of their thermodynamic properties in aqueous solutions is very important to understand various industrial and geochemical processes such as crystallization, evaporite formation and subsurfaces brine evolution. In particular, vapor-liquid equilibrium (VLE) data are needed to design separation processes such as distillation and evaporation but are also important thermodynamic properties. Calorimetric data, including enthalpies and heat capacities, are mainly used by industrials for the calculation of thermal effects linked to dissolution of solids in liquid phase and mixture or heating and crystallization. However, from a theoretical point of view, they are related to derivatives of equilibrium properties with respect to temperatures (according to the Gibbs - Helmoltz relationship) and are consequently very important for modeling thermodynamic properties of solutions.

Though numerous experimental and theoretical investigations have been reported on binaries  $\{NaCl + H_2O\}$ (see for example, Clarke and Glew<sup>6</sup>) and  $\{Na_2SO4 + H_2O\}$ (see, for example, Marliacy et al.<sup>7</sup> and references therein), much less data exists on the {NaCl + Na<sub>2</sub>SO<sub>4</sub> +  $H_2O$ } ternaries. Thus, Tischenko et al.8 made measurements of mean activity coefficients of NaCl and Na<sub>2</sub>SO<sub>4</sub> in water at various composition between 278 and 318 K. However, most VLE data on this system were reported at 298 K; the reports concern the determination of osmotic coefficients by isopiestic methods (Robinson et al.,<sup>9</sup> Platford,<sup>10</sup> and Wu et al.<sup>11</sup>) or the direct measurements of activity coefficients from electrochemical techniques (Synott and Buttler<sup>12</sup> and Lanier<sup>13</sup>). Similarly, calorimetric data of aqueous {Na<sub>2</sub>SO<sub>4</sub> + NaCl} are very scarce; heats of mixing measurements of sodium sulfate and sodium chloride solutions were reported by Snra and Wood<sup>14</sup> at ambient temperature, and more recently. Conti et al.<sup>15</sup> measured isobaric heat capacities for aqueous solutions containing the system Na-K-Cl-SO4 from 333 K to 473 K.

The determination of activities of solutes (Na<sup>+</sup>, Cl<sup>-</sup>, and SO<sub>4</sub><sup>2–</sup>) or activity of water can be made using isopiestic methods (Hefter et al.<sup>16</sup>) or by direct measurements of vapor pressures. Although less precise than the isopiestic method, the latter technique is often preferred especially when the volatility of electrolytes can be neglected and because it requires only a short time to reach equilibrium conditions. Vapor pressures in binary {NaCl +  $H_2O$ } systems were measured in this way with the help of a nonisothermal static device constructed in our laboratory (Hubert et al.<sup>1</sup>). The possible extension of this apparatus to a more complex system was tested in this work. We made vapor pressure measurements in the ternary {NaCl  $(1) + Na_2SO_4(2) + H_2O(3)$  system between (298 and 363) K with different molality ratios  $m_1/m_2 = 1/10$  and  $m_1/m_2$ = 1/1. Data obtained at constant composition could be easily used for determining coefficients of Appelblatt's correlation.<sup>2</sup>

Numerous experimental techniques have been proposed (Marsh and O'Hare<sup>17</sup>) to measure enthalpies of dissolution, enthalpies of dilution, or heat capacities. Particularly, it has been shown that dissolution enthalpy of sodium chloride (Hubert et al.18) and sodium sulfate (Hubert et al.<sup>19</sup>) performed in a mixing differential calorimeter can be used for expressing variations with respect to temperature of binary interaction parameters in an excess Gibbs energy model proposed by Pitzer.<sup>3</sup> The proposed methodology leads to a set of binary parameters which allows very accurate calculations of mean activity coefficients, activity of water and dissolution enthalpies for binary  $\{H_2O + Na_2SO_4 \text{ or }$ NaCl } systems (Marliacy et al.<sup>20</sup>). Similar results have been obtained with an NRTL electrolyte model proposed by Chen and co-workers (Chen et al.<sup>4,5</sup>) for binary  $\{H_2O +$  $Na_2SO_4$  system (Marliacy et al.<sup>7</sup>). In the present paper, this method will be applied to more complex systems. Ternary interaction parameters of Pitzer and Chen's models will be determined using dissolution enthalpies of both anhydrous NaCl and Na<sub>2</sub>SO<sub>4</sub> in pure water up to saturation at 297.75 K, 317.45 K, and 332.35 K (with molality ratios  $m_1/m_2 = 1/10$ ,  $m_1/m_2 = 1/1$ , and  $m_1/m_2 =$ 

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**Figure 1.** Schematic description of our non isothermal static device for measuring vapor pressure in electrolyte solutions.

10/1, respectively) and using solubility data at 298.15 K for the ternary system. Finally, we will test the thermodynamic consistency of our parameters by calculating both dissolution enthalpies and activities of water in the {NaCl (1) + Na<sub>2</sub>SO<sub>4</sub> (2) + H<sub>2</sub>O (3)} system. A systematic comparison of results obtained with both models will be performed.

## 2. Experimental Section

Reagent grade  $Na_2SO_4$  and NaCl (Aldrich) were used with a purity greater than 99%. They were previously dried at 383.15 K and stored in a desiccator next to a vessel containing highly concentrated  $H_2SO_4$ . The water was demineralized and twice distilled.

**2.1. Vapor Pressure Measurements.** Vapor pressures were measured in a nonisothermal static device built in our laboratory.<sup>1</sup> A schematic description of this apparatus is shown in Figure 1. An aqueous electrolytes liquid solution of known composition is introduced into a thermostated cell. Then, the equilibrium pressure above the liquid solution is measured at different temperatures with a manometer placed in an external jacket thermostated at a high temperature (403.15 K) to ensure a good thermal stability of the sensor. With this type of apparatus pressure measurements were performed as a function of temperature at a constant liquid composition.

Temperature of the gas–liquid interface in the cell is measured within  $\pm 0.01$  K with a Pt 100 thermometer. An absolute manometer (MKS Baratron 315 B, 0 to 1000 Torr) allows the determination of the pressure with an accuracy of  $\pm 0.1\%$ . The composition of liquid mixture is determined at  $\pm 0.001$  mol·kg<sup>-1</sup> with a vibrating tube densimeter (ANTON PAAR, DMA 45).

Calibration of the densimeter was made at 298.15  $\pm$  0.02 K using two different reference solutions in which  $m_1 = m_2$  and  $m_1/m_2 = 1/10$ . For each type of solution, measurement of the vibrating period,  $\tau$ , leads to the determination of molalities  $m_1$  and  $m_2$  according to

$$m_{i} = A_{i}(\tau - \tau_{w}) + B_{i}(\tau - \tau_{w})^{2} + C_{i}(\tau - \tau_{w})^{3}$$
(1)

in which  $\tau_w$  is the vibrating period of water and  $A_i$ ,  $B_j$ , and  $C_i$  are constants fitted from compositions of reference solutions. Measurements of vapor pressures of pure water between (273.15 and 368.15) K were made to test the apparatus. The agreement between our experimental values and those reported by Haar et al.<sup>21</sup> is better than 0.1%.

Measurements were performed between (298 and 363) K with 8 solutions in which  $m_1 = m_2$  (from 0.2625 to 1.04915 mol·kg<sup>-1</sup>) and 7 solution with  $m_1/m_2 = 1/10$  (m<sub>2</sub> =



**Figure 2.** Molal dissolution enthalpy  $(J \cdot kg^{-1})$  of {NaCl (1) + Na<sub>2</sub>-SO<sub>4</sub> (2)} mixtures in water ( $m_1/m_2 = 10/1$ ).

0.2448 to 1.3596 mol·kg<sup>-1</sup>) corresponding to ionic strengths from 0.77 to 4.214 mol/kg<sup>-1</sup>. Values of pressures are reported in Table 1.

**2.2. Dissolution Enthalpy Measurements.** Dissolution enthalpies were measured using a SETARAM C80D differential calorimeter. Known masses of solid sodium chloride, solid sodium sulfate, and water were introduced in the two parts of the mixing cell. The reference cell was filled with a mass of water equal to the sum of three previous ones. The working temperature was fixed, and when thermal equilibrium was reached, the mixing was achieved using an inverting mechanism driven by an electric motor. The accuracy of the mass measurements was about of  $\pm 0.1$  mg. The sensitivity of this calorimeter slightly decreases with temperature and is  $31.5 \,\mu V \cdot m W^{1-}$  at 290 K and 29.5  $\mu V \cdot m W^{1-}$  at 390 K.

The lower value of the salt molality was chosen according to the calorimeter's sensitivity. The reproducibility of the experiments has been tested using two series of measurements made with {H<sub>2</sub>O + NaCl} in the molality range from 0.05 mol·kg<sup>-1</sup> to 6.0 mol·kg<sup>-1</sup> at 317.45 K. A relative mean deviation of about 1.5% was found between the two data sets.

Measurements were performed at respectively 297.8 K, 317.5 K, and 332.4 K in solutions of NaCl (1) and Na<sub>2</sub>SO<sub>4</sub> (2) in which the ratio  $m_1/m_2$  is respectively equal to 1/10(with  $m_2 \approx 0.41 - 3.0 \text{ mol} \cdot \text{kg}^{-1}$ ), to 1 (with  $m_2 \approx 0.26 - 1.9$ mol·kg<sup>-1</sup>), and to 10/1 (with  $m_1 \approx 0.36-5.1$  mol·kg<sup>-1</sup>) corresponding to ionic strengths from approximately 0.40 to 9.3 mol/kg<sup>-1</sup>. The experimental results of our dissolution experiments are reported in Table 2. Molal dissolution enthalpies (in J/kg of water) at  $m_1/m_2 = 10/1$ ,  $m_1/m_2 = 1$ , and  $m_1/m_2 = 1/10$  are plotted against ionic strength in respectively Figures 2-4. Inspection of these data leads to the conclusion that values obtained in the ternary system 1/10 are nearly identical to those obtained in binary  $\{Na_2SO_4 + H_2O\}$ ;<sup>7</sup> this is due to the fact that ionic strength of the ternary solution strongly depends on the molality of sodium sulfate ( $I = m_1 + 3m_2$ ). Moreover, dissolution of mixtures in which  $m_1 > m_2$  are endothermic and at the opposite, solutions in which  $m_2 > m_1$  present highly negative dissolution enthalpies.

## 3. Results and Discussions

**3.1.** Determination of Activity of Water from Pressure Measurements. It is possible to demonstrate (see for example<sup>1</sup>) that activity of water,  $a_w$ , in a nonvolatile electrolyte aqueous solution at temperature *T* can be directly related to equilibrium pressure above liquid, *P*, and

Table 1. Vapor Pressures  $P_{exp}$ , and Activities of Water,  $a_w$ , in {NaCl (1) + Na<sub>2</sub>SO<sub>4</sub> (2) + H<sub>2</sub>O (3)} with  $m_1/m_2 = 1/10$  and  $m_1/m_2 = 1$ 

T	Pexp		a <sub>w</sub>	T	Pexp		$a_{\rm w}$		$P_{\rm exp}$		$a_{\rm w}$	T	$P_{\rm exp}$		$a_{\rm w}$
K	Pa	$a_w$	Appelblat	K	Pa	$a_{\rm w}$	Appelblat	K	Pa	$a_w$	Appelblat	K	Pa	$a_{\scriptscriptstyle \mathrm{W}}$	Appelblat
298.67 303.46 308.32 313.14	3097.1 4094.3 5376.9 6982.6	0.9487 0.9484 0.9475 0.9473	0.9486 0.9483 0.9480 0.9478	m 317.97 322.79 327.72 332.64	$p_1 = 0.133$ 9001.6 11486 14612 18412	596 mol·k 0.9482 0.9479 0.9480 0.9467	$xg^{-1}, m_2 = 1$ 0.9476 0.9475 0.9474 0.9473	.3596 m 337.58 342.52 347.40 352.33	ol•kg <sup>-1</sup> 23078 28704 35384 43383	$m_1/m_2 = 0.9468 \\ 0.9468 \\ 0.9476 \\ 0.9475$	1/10 0.9473 0.9473 0.9473 0.9473 0.9474	357.27 362.13	52902 63835	0.9479 0.9472	0.9475 0.9476
298.56 303.40 308.22 313.06	3086.9 4093.9 5367.6 6983.7	0.9513 0.9514 0.9514 0.9514	0.9515 0.9513 0.9512 0.9512	m 317.95 322.78 327.61 332.45	$p_1 = 0.127$ 9022.3 11513 14582 18334	715 mol·k 0.9515 0.9508 0.9511 0.9508	${ m ag}^{-1},\ m_2=1\ 0.9512\ 0.9512\ 0.9513\ 0.9513\ 0.9514$	.2715 mc 337.31 342.24 347.08 352.00	ol·kg <sup>-1</sup> 22915 28506 35082 43038	$m_1/m_2 = 0.9516 \\ 0.9519 \\ 0.9522 \\ 0.9526$	1/10 0.9515 0.9517 0.9519 0.9521	356.89 361.75	52363 63237	0.9524 0.9522	0.9524 0.9527
298.82 303.66 308.49 313.35	3178.3 4216.5 5526.7 7192.4	$0.9647 \\ 0.9655 \\ 0.9649 \\ 0.9649$	$\begin{array}{c} 0.9651 \\ 0.9650 \\ 0.9649 \\ 0.9649 \end{array}$	m 318.24 323.03 327.89 332.77	$h_1 = 0.088$ 9289.9 11829 15004 18871	349 mol·k 0.9651 0.9648 0.9651 0.9646	${ m kg}^{-1}, m_2 = 0 \ 0.9649 \ 0.9649 \ 0.9650 \ 0.9650$	0.8849 m 337.69 342.63 347.49 352.43	ol·kg <sup>-1</sup> 23630 29398 36208 44416	$m_1/m_2 = 0.9647 \\ 0.9651 \\ 0.9658 \\ 0.9660$	1/10 0.9652 0.9653 0.9654 0.9656	357.38 362.26	54174 65403	0.9663 0.9655	0.9658 0.9660
298.38 303.27 308.08 312.97	3112.3 4139.6 5425.9 7079.1	$0.9697 \\ 0.9694 \\ 0.9690 \\ 0.9692$	0.9697 0.9695 0.9693 0.9691	m 317.92 322.73 327.60 332.49	$h_1 = 0.080$ 9178.0 11704 14852 18700	081 mol·k 0.9695 0.9688 0.9688 0.9688 0.9680	${ m kg}^{-1},  m_2 = 0 \\ 0.9689 \\ 0.9688 \\ 0.9688 \\ 0.9688 \\ 0.9688 \end{cases}$	0.8081 m 337.44 342.39 347.28 352.22	ol·kg <sup>-1</sup> 23465 29203 36016 44186	$m_1/m_2 = 0.9686 \\ 0.9689 \\ 0.9692 \\ 0.9692 \\ 0.9692$	1/10 0.9688 0.9688 0.9688 0.9689	357.14 362.06	53806 65137	0.9690 0.9689	0.9690 0.9692
298.47 303.39 308.27 313.12	3159.7 4215.4 5544.8 7213.9	0.9791 0.9802 0.9796 0.9798	0.9799 0.9797 0.9795 0.9794	n 318.04 322.84 327.70 332.60	$a_1 = 0.053$ 9336.0 11896 15081 19000	524 mol·ł 0.9798 0.9793 0.9789 0.9784	${ m kg}^{-1}, m_2 = 0 \ 0.9793 \ 0.9793 \ 0.9793 \ 0.9793 \ 0.9793 \ 0.9793 \ 0.9793$	.5524 mc 337.56 342.51 347.42 352.36	ol·kg <sup>-1</sup> 1 23842 29686 36621 44941	$m_1/m_2 = 0.9791 \\ 0.9794 \\ 0.9797 \\ 0.9799 \\ 0.9799$	1/10 0.9793 0.9794 0.9795 0.9797	357.29 362.18	54764 66174	0.9801 0.9798	0.9798 0.9800
298.64 303.50 308.36 313.21	3214.1 4266.3 5602.0 7288.5	0.9858 0.9857 0.9852 0.9850	0.9859 0.9855 0.9852 0.985	m 318.09 322.91 327.78 332.66	$h_1 = 0.040$ 9410.0 11997 15219 19149	046 mol·k 0.9850 0.9845 0.9841 0.9836	${ m kg}^{-1},  m_2 = 0 \ 0.9848 \ 0.9847 \ 0.9846 \ 0.9845$	.4046 mc 337.61 342.58 347.47 352.42	ol·kg <sup>-1</sup> 24035 29937 36916 45302	$m_1/m_2 = 0.9847 \\ 0.9850 \\ 0.9855 \\ 0.9856$	1/10 0.9846 0.9846 0.9847 0.9849	357.35 362.24	55160 66666	0.9848 0.9847	0.9851 0.9853
298.77 303.59 308.42 313.28	3252.8 4308.0 5647.5 7346.8	0.9900 0.9902 0.9896 0.9893	0.9901 0.9899 0.9896 0.9895	m 318.17 322.97 327.81 327.81	$p_1 = 0.024$ 9492.2 12088 15314 15314	484 mol·k 0.9896 0.9890 0.9891 0.9891 0.9891	$g^{-1}, m_2 = 0$ 0.9893 0.9892 0.9892 0.9892 0.9892	0.2484 m 332.69 337.62 342.55 347.40	ol·kg <sup>-1</sup> 19278 24156 30042 36980	$m_1/m_2 = 0.9889 \\ 0.9891 \\ 0.9895 \\ 0.9900$	1/10 0.9892 0.9893 0.9894 0.9895	352.35 357.29	45379 55320	0.9899 0.9901	0.9897 0.9899
298.34 303.16 307.96 312.79	2967.5 3931.0 5150.7 6700.0	0.9270 0.9266 0.9261 0.9262	0.9271 0.9266 0.9263 0.9260	317.66 322.50 327.34 332.22	$m_1 = 1.04$ 8655.9 11057 14009 17646	495 mol·k 0.9265 0.9260 0.9258 0.9254	${ m ag}^{-1}, m_2 = 1 \\ 0.9259 \\ 0.9259 \\ 0.9259 \\ 0.9259 \\ 0.9260$	.0495 mc 337.12 342.03 346.88 351.80	ol·kg <sup>-1</sup> 22108 27493 33851 41531	$m_1/m_2 = 0.9261 \\ 0.9266 \\ 0.9270 \\ 0.9272$	1/1 0.9262 0.9265 0.9268 0.9272	356.70 361.59	50601 61254	0.9276 0.9283	0.9277 0.9282
298.35 303.16 307.98 312.84	2992.0 3960.5 5193.9 6764.7	0.9338 0.9333 0.9326 0.9325	0.9338 0.9333 0.9329 0.9326	317.77 322.59 327.43 332.30	$m_1 = 0.97$ 8767.8 11187 14175 17839	775 mol·k 0.9332 0.9326 0.9323 0.9320	${ m ag}^{-1},\ m_2=0\ 0.9324\ 0.9323\ 0.9322\ 0.932\ 0$	0.9775 m 337.24 342.17 347.03 351.96	ol·kg <sup>-1</sup> 22358 27831 34282 42073	$m_1/m_2 = 0.9318 \\ 0.9324 \\ 0.9326 \\ 0.9329$	1/1 0.9323 0.9324 0.9326 0.9329	356.89 361.84	51298 62218	0.9331 0.9337	0.9332 0.9335
298.38 303.27 308.08 312.95	3004.3 3991.8 5228.3 6806.2	0.9359 0.9348 0.9339 0.9329	0.9360 0.9348 0.9339 0.9331	317.85 322.65 327.51 332.40	$m_1 = 0.96 \\ 8800.5 \\ 11211 \\ 14222 \\ 17911$	317 mol·k 0.9327 0.9321 0.9318 0.9312	${ m ag}^{-1},\ m_2=0\ 0.9325\ 0.9320\ 0.9317\ 0.9316$	.9617 mc 337.33 342.26 347.13 352.07	ol·kg <sup>-1</sup> 22440 27921 34406 42230	$m_1/m_2 = 0.9315 \\ 0.9317 \\ 0.9319 \\ 0.9324$	1/1 0.9316 0.9317 0.9319 0.9323	357.04 361.97	51584 62491	0.9328 0.9332	0.9327 0.9333
298.42 303.19 308.06 312.90	3042.9 4019.7 5289.1 6878.1	0.9461 0.9454 0.9454 0.9454	0.9460 0.9457 0.9455 0.9453	317.79 322.61 327.45 332.33	$m_1 = 0.79$ 8894.3 11348 14387 18113	901 mol·k 0.9456 0.9455 0.9452 0.9450	${ m g}^{-1},\ m_2=0\ 0.9452\ 0.9452\ 0.9453\ 0.9453\ 0.9454$	0.7901 m 337.24 342.19 347.08 352.02	ol•kg <sup>-1</sup> 22689 28255 34856 42789	$m_1/m_2 = 0.9453 \\ 0.9457 \\ 0.9462 \\ 0.9464$	1/1 0.9455 0.9458 0.9460 0.9464	356.97 361.87	52211 63206	0.9467 0.9471	0.9467 0.9471
298.32 303.14 307.99 312.84	3052.1 4045.1 5317.5 6923.6	0.9546 0.9545 0.9544 0.9543	0.9548 0.9545 0.9543 0.9541	317.75 322.57 327.42 332.28	$m_1 = 0.66$ 8960.1 11432 14494 18244	351 mol·k 0.9545 0.9539 0.9540 0.9537	${ m g}^{-1},\ m_2=0\ 0.9540\ 0.9540\ 0.9541\ 0.9541\ 0.9542$	.6651 m 337.21 342.17 347.05 351.95	ol•kg <sup>-1</sup> 22870 28495 35135 43077	$m_1/m_2 = 0.9542 \\ 0.9546 \\ 0.9550 \\ 0.9553$	1/1 0.9544 0.9546 0.9549 0.9552	356.90 361.83	52551 63701	0.9554 0.9560	0.9555 0.9559
298.31 303.12 307.94 312.75	3082.9 4082.7 5357.7 6965.3	0.9648 0.9644 0.9644 0.9647	0.9651 0.9647 0.9644 0.9642	317.67 322.51 327.35 332.23	$m_1 = 0.52 \\9018.2 \\11518 \\14604 \\18396$	204 mol·k 0.9648 0.9641 0.9641 0.9639	${ m kg}^{-1},  m_2 = 0 \ 0.9641 \ 0.9641 \ 0.9642 \ 0.9644 \ 0.9644$	.5204 m 337.18 342.12 347.03 351.98	ol•kg <sup>-1</sup> 23079 28744 35488 43620	$m_1/m_2 = 0.9641 \\ 0.9648 \\ 0.9652 \\ 0.9662$	1/1 0.9646 0.9649 0.9653 0.9658	356.93 361.87	53207 64535	0.9661 0.9669	0.9662 0.9668
298.33 303.13 307.97 312.82	3107.2 4112.9 5403.4 7036.0	0.9710 0.9708 0.9708 0.9711	0.9707 0.9709 0.9711 0.9712	317.69 322.53 327.37 332.25	$m_1 = 0.40$ 9090.6 11618 14727 18559	073 mol·k 0.9718 0.9715 0.9715 0.9715 0.9717	${ m g}^{-1},  m_2 = 0 \ 0.9714 \ 0.9716 \ 0.9717 \ 0.9719$	.4073 mo 337.17 342.10 346.97 351.89	ol•kg <sup>-1</sup> 23260 28945 35669 43772	$m_1/m_2 = 0.9720 \\ 0.9724 \\ 0.9726 \\ 0.9731$	1/1 0.9721 0.9722 0.9724 0.9725	356.81 361.65	53323 64336	0.9729 0.9721	0.9727 0.9728
298.35 303.14 308.00 312.82	3149.4 4166.9 5479.2 7120.8	0.9828 0.9828 0.9826 0.9827	0.9825 0.9827 0.9828 0.9829	317.71 322.51 327.35 332.21	$m_1 = 0.26$ 9207.0 11746 14894 18741	625 mol·k 0.9831 0.9830 0.9832 0.9831	${ m kg}^{-1}, m_2 = 0 \ 0.9831 \ 0.9832 \ 0.9834 \ 0.9835$	.2625 m 337.13 342.10 346.96 351.89	ol•kg <sup>-1</sup> 23497 29296 36092 44294	$m_1/m_2 = 0.9837$ 0.9842 0.9844 0.9846	1/1 0.9837 0.9838 0.9840 0.9841	356.81 361.64	53972 65071	0.9846 0.9835	0.9843 0.9844

Table 2. Molal Dissolution Enthalpies  $\Delta_{sol}\hat{H}$  of NaCl (1) and Na<sub>2</sub>SO<sub>4</sub> (2) in Water at 297.75 K, 317.45 K, and 332.35 K with  $m_1/m_2 = 1/10$ ,  $m_1/m_2 = 1$ , and  $m_1/m_2 = 10/1'$ 

mol·	kg <sup>-1</sup>		$\Delta_{sol}\hat{H}$	mol·	kg <sup>-1</sup>		$\Delta_{\rm sol} \hat{H}$
$m_1$	$m_2$	$m_1/m_2$	J•kg <sup>-1</sup>	$m_1$	$m_2$	$m_1/m_2$	J·kg <sup>-1</sup>
			$T = 29^{\circ}$	7.75 K			
0.0414	0.4139	1/10	-1038.3	0.2001	2.0000	1/10	-16644
0.0827	0.8264	1/10	-3782.2	0.2399	2.3992	1/10	-21779
0.1245	1.2447	1/10	-7733.2	0.2800	2.7999	1/10	-26740
0.1659	1.6587	1/10	-12609	0.3000	3.0002	1/10	-29011
			T = 31	7.45 K			
0.0414	0.4139	1/10	-2311.5	0.2000	1.9995	1/10	-16195
0.0826	0.8263	1/10	-5235.2	0.2399	2.3991	1/10	-20136
0.1170	1.1702	1/10	-8330.5	0.2800	2.8001	1/10	-23259
0.1657	1.6567	1/10	-12839	0.3000	2.9996	1/10	-25268
			T = 332	2.35 K			
0.0414	0.4137	1/10	-3145.1	0.2000	2.0003	1/10	-16149
0.0826	0.8264	1/10	-6367.9	0.2400	2.3994	1/10	-19291
0.1244	1.2444	1/10	-9767.6	0.2800	2.7997	1/10	-21923
0.1656	1.6559	1/10	-13190	0.3000	3.0005	1/10	-22484
			$T = 29^{\circ}$	7.75 K			
0.2602	0.2602	1	339.87	1.2008	1.2008	1	-6566.2
0.5501	0.5500	1	-748.53	1.4001	1.4001	1	-8817.0
0.7721	0.7721	1	-2416.9	1.6507	1.6506	1	-11657
0.9896	0.9896	1	-4377.0	1.8513	1.8513	1	-13881
			T = 31	7.45 K			
0.3000	0.3000	1	-1119.4	1.2461	1.2460	1	-7874.3
0.5501	0.5501	1	-2470.8	1.4521	1.4521	1	-9627.4
0.7917	0.7917	1	-4200.7	1.7010	1.7010	1	-11505
1.0194	1.0194	1	-6019.0	1.9008	1.9007	1	-12838
			T = 33	2.35 K			
0.2429	0.2429	1	-1642.1	1.1595	1.1595	1	-7987.8
0.5001	0.5001	1	-3221.3	1.3812	1.3812	1	-9583.7
0.7203	0.7203	1	-4834.1	1.6012	1.6012	1	-10699
0.9404	0.9404	1	-6387.4	1.8002	1.8001	1	-11817
0.0500	0.0050	10/1	$T = 29^{\circ}$	7.75 K	0 0050	10/1	1075 0
0.3596	0.0359	10/1	1497.7	3.3540	0.3353	10/1	4975.2
0.8215	0.0823	10/1	2937.6	4.0547	0.4055	10/1	4829.5
1.2323	0.1232	10/1	3822.9	4.4043	0.4404	10/1	4730.1
1.6408	0.1641	10/1	4386.0	4.7531	0.4752	10/1	4960.0
2.1670	0.2168	10/1	4857.2	4.9378	0.4938	10/1	4896.8
2.6521	0.2651	10/1	4988.1	5.1240	0.5124	10/1	4993.4
			T = 31	7.45 K			
0.3579	0.0358	10/1	660.95	3.4265	0.3426	10/1	2833.7
0.8232	0.0823	10/1	1357.4	3.8141	0.3814	10/1	3074.0
1.3972	0.1397	10/1	1939.6	3.9082	0.3908	10/1	2810.7
2.0882	0.2088	10/1	2461.5	4.2001	0.4200	10/1	3333.5
2.6362	0.2635	10/1	2691.1	4.4026	0.4398	10/1	3776.5
3.1001	0.3100	10/1	2697.3	4.6385	0.4639	10/1	3847.2
3.4248	0.3426	10/1	2818.3	4.7686	0.4769	10/1	4034.4
				4.8997	0.4900	10/1	4181.8
			T = 332	2.35 K			
0.4041	0.0404	10/1	109.18	3.2763	0.3276	10/1	1221.6
0.7642	0.0764	10/1	254.01	3.6389	0.3639	10/1	1585.7
1.2000	0.1200	10/1	388.87	4.0006	0.4001	10/1	1901.6
1.5873	0.1587	10/1	524.72	4.3012	0.4301	10/1	2348.7
1.9718	0.1972	10/1	651.48	4.5805	0.4581	10/1	2836.9
2.5003	0.2500	10/1	904.57	4.7502	0.4750	10/1	3160.0
2.9158	0.2916	10/1	1013.7	5.0074	0.5007	10/1	3858.5

vapor pressure of pure water at T,  $P_{w}^{i}$ , according to the relationship,

$$\ln a_{\rm w} = \ln\left(\frac{P}{P_{\rm w}^{\rm s}}\right) + \frac{(P - P_{\rm w}^{\rm s})}{RT}(B - v_{\rm w}^{\rm s}) = \ln\left(\frac{P}{P_{\rm w}^{\rm s}}\right) + \delta \tag{2}$$

in which the corrective term  $\delta$  is defined with *B*, the second virial coefficient of water (Le Fevre et al.<sup>22</sup>), and  $v_w^*$ , the molar volume of pure liquid water (Kell<sup>23</sup>). Values of  $\delta$  are very small (they do not exceed 0.2% of the  $P/P_w^*$ ) but must be taken into account because they have the same order of magnitude as our experimental accuracy (0.1%). Values of  $a_w$  obtained using eq 2 are reported together with experimental values of P in the Table 1.



**Figure 3.** Molal dissolution enthalpy  $(J \cdot kg^{-1})$  of {NaCl (1) + Na<sub>2</sub>-SO<sub>4</sub> (2)} mixtures in water ( $m_1/m_2 = 1/1$ ); comparison with model of Pitzer (calculation with Chen's model gives same results).



**Figure 4.** Molal dissolution enthalpy  $(J \cdot kg^{-1})$  of {NaCl (1) + Na<sub>2</sub>-SO<sub>4</sub> (2)} mixtures in water ( $m_1/m_2 = 1/10$ ); comparison with model of Pitzer (calculation with Chen's model gives same results).

For each composition, experimental results can be regressed using the Appelblatt relation,<sup>2</sup> given by

$$\ln(P_{\rm w}^{\rm s} - P) = A + \frac{B}{T} + C \left( \ln(T) - \frac{T}{2T_{\rm c}} \right)$$
(3)

where *T* is absolute temperature in K,  $T_c$  is the critical temperature of water ( $T_c = 647.14$  K), and *A*, *B*, and *C* are adjustable parameters depending on liquid composition. Values of these parameters were regressed on our experimental values of pressure for each ternary composition studied and are reported in the Table 3. A strong correlation between these parameters can be observed. As it can be observed, deviations between experimental and calculated values of  $a_w$  are very low (<0.1%). It is also clearly evident that, for a given composition, the influence of temperature on activity of water is negligible.

**3.2.** Modeling with Pitzer and Chen Electrolyte Models. Thermodynamic Background. Excess Gibbs energy models for aqueous electrolyte solutions can be used to correlate our experimental dissolution enthalpy and activity of water data. The expressions proposed by Pitzer<sup>3</sup> and by Chen et al.<sup>4,5</sup> are extensively used in the literature and can be applied successfully in this work. In the two models, excess Gibbs energy of a solution can be considered as a sum of a Pitzer–Debye–Hückel term which expresses the effect of long-range interactions between ions and a second term accounting for the short-range interactions between solute species.

Table 3. *A*, *B*, and *C* Parameters of Appelblatt's Expression (eq 2) at Different Molalities of NaCl and Na<sub>2</sub>SO<sub>4</sub> (with  $m_1/m_2 = 1/10$  and  $m_1/m_2 = 1$ , Respectively)

$m_1/\text{mol}\cdot\text{kg}^{-1}$	$m_2/\text{mol}\cdot\text{kg}^{-1}$	$m_1/m_2$	Α	В	С
0.13596	1.3596	1/10	109.76	-8604.18	-13.87
0.12715	1.2715	1/10	117.79	-8852.77	-15.40
0.08849	0.8849	1/10	118.73	-8901.34	-15.40
0.08081	0.8081	1/10	130.01	-9411.64	-17.17
0.05524	0.5524	1/10	162.55	-10655.61	-22.43
0.04046	0.4046	1/10	257.03	-14421.91	-37.47
0.02484	0.2484	1/10	309.35	-16421.00	-45.88
1.0495	1.0495	1	139.26	-9686.27	-18.53
0.9775	0.9775	1	131.88	-9432.49	-17.36
0.9617	0.9617	1	193.28	-11877.38	-27.09
0.7901	0.7901	1	140.09	-9723.56	-18.71
0.6651	0.6651	1	153.48	-10244.16	-20.88
0.5204	0.5204	1	209.46	-12395.12	-29.85
0.4073	0.4073	1	77.96	-7250.40	-8.98
0.2625	0.2625	1	95.29	-7886.04	-11.86

In the equation proposed by Pitzer,<sup>3</sup> the molal excess Gibbs energy (in J/kg of water),  $\hat{G}^{\rm E}$ , is defined in molality scale and in unsymmetric convention like a function of  $m_{\rm c}$ ,  $m_{\rm a1}$ , and  $m_{\rm a2}$ , respectively, the molalities of cation Na<sup>+</sup>, of anion Cl<sup>-</sup>, and of anion SO<sub>4</sub><sup>2-</sup> which can be easily calculated from the apparent molality of salt,  $m_1$  and  $m_2$ ,

 $m_{\rm c} = m_1 + 2m_2$ ,  $m_{\rm a1} = m_1$ , and  $m_{\rm a2} = m_2$ 

if the hypothesis of complete dissociation of electrolytes is made. The short-range interactions term is a virial development of molalities of species.

The model of Chen and co-workers<sup>5</sup> is an expression of the molar excess Gibbs energy (in J/mol of true species),  $G_{\rm m}^{\rm E}$ , in unsymmetric convention and in molar fraction scale. Its second term is accounted for by the NRTL theory and is based on the local composition concept. Under the same hypothesis of complete dissociation, true molar fractions of Na<sup>+</sup>,  $x_{\rm c}$ , of Cl<sup>-</sup>,  $x_{\rm a1}$ , of SO<sub>4</sub><sup>2-</sup>,  $x_{\rm a2}$ , and of water,  $x_{\rm w}$ , can also be expressed from apparent molalities of electrolytes,

$$x_{\rm w} = \frac{\frac{1000}{M_{\rm W}}}{\frac{1000}{M_{\rm w}} + (m_1 + 2m_2) + m_1 + m_2},$$
$$x_{\rm c} = \frac{m_1 + 2m_2}{\frac{1000}{M_{\rm w}} + (m_1 + 2m_2) + m_1 + m_2}$$

$$x_{a1} = \frac{m_1}{\frac{1000}{M_w} + (m_1 + 2m_2) + m_1 + m_2}},$$
$$x_{a2} = \frac{m_2}{\frac{1000}{M_w} + (m_1 + 2m_2) + m_1 + m_2}}$$

In which  $M_{\rm w} = 18.0153 \, {\rm g} \cdot {\rm mol}^{-1}$  is the molar mass of water. Classical thermodynamic properties (such as activity and osmotic coefficients) can be derived from the expressions of  $G^{\rm E}$ . They can be found in the papers of the authors.<sup>1,5</sup> However, some general equations can be given to precise how they can be obtained. Expression of thermodynamic properties usually depend on the choice of reference state. Thus, activity coefficients of species,  $\gamma_{i}$  are obtained using the general relationship

$$RT\ln\gamma_i = \left(\frac{\partial G^{\rm E}}{\partial \mathbf{n}_i}\right)_{T,P,nj\neq i} \tag{4}$$

where  $n_i$  is the amount of species *i*.

In molar fraction scale (for Chen's model) :

$$G^{\rm E} = (n_{\rm w} + n_{\rm c} + n_{\rm a1} + n_{\rm a2}) G_{\rm m}^{\rm E}$$
 (5)

In molality scale (for Pitzer's model):

$$G^{\rm E} = n_{\rm w} \frac{M_{\rm W}}{1000} \hat{G}^{\rm E}$$
 (6)

Activity of water,  $a_w$ , is calculated from activity coefficient of water in the solution,  $\gamma_w$ :

In molar fraction scale (for Chen's model):  $\ln a_{\rm w} = \ln \gamma_{\rm w} + \ln x_{\rm w} (7)$ 

In molality scale (for Pitzer's model):

$$\ln a_{\rm w} = \ln \gamma_{\rm w} - \frac{M_{\rm W}}{1000} (m_{\rm c} + m_{\rm a1} + m_{\rm a2}) \quad (8)$$

The activity of water is usually expressed by the osmotic coefficient  $\boldsymbol{\Phi},$ 

$$\Phi = -\frac{1000}{M_{\rm w}} \frac{\ln a_{\rm w}}{m_{\rm c} + m_{\rm a1} + m_{\rm a2}} \tag{9}$$

The thermal effect measured when  $n_1$  moles of NaCl and  $n_2$  moles of sodium sulfate are dissolved in  $n_w = n_3$  moles of water, noted  $\Delta_{sol}H$ , is related to excess enthalpy defined in unsymmetric convention,  $H^{\text{E}\ 18,19}$  according to

$$\Delta_{\rm sol} H = n_1 \Delta_{\rm sol} H_{m,1}^{\circ} + n_2 \Delta_{\rm sol} H_{m,2}^{\circ} + H^{\rm E}(n_1, n_2, n_{\rm w}) \quad (10)$$

in which  $\Delta_{sol}H_{m,1}^{\circ}$  and  $\Delta_{sol}H_{m,2}^{\circ}$  are the molar dissolution enthalpy of NaCl and Na<sub>2</sub>SO<sub>4</sub> at infinite dilution. Excess enthalpy can be calculated from the excess Gibbs energy models using the Gibbs–Helmholtz relationship,

$$H^{\rm E} = -T^2 \left( \frac{\partial (G^{\rm E}/T)}{\partial T} \right)_{P,n_i} \tag{11}$$

Finally, the molal dissolution enthalpy,  $\Delta_{sol}\hat{H}$ , i.e., excess enthalpy of an aqueous solution containing two electrolytes of apparent molalities  $m_1$  and  $m_2$  and 1 kg of water, is calculated by,

$$\Delta_{\rm sol}\hat{H} = \frac{\Delta_{\rm sol}H}{n_{\rm w}\frac{M_{\rm w}}{1000}} \tag{12}$$

**Determination of Pitzer's and Chen's Parameters.** Excess Gibbs energy models proposed either by Pitzer or by Chen and co-workers are under the dependence of some binary and ternary adjustable parameters.

Most of binary parameters are temperature dependent and must be fitted on thermodynamic properties of binary {NaCl + H<sub>2</sub>O} or {Na<sub>2</sub>SO<sub>4</sub> + H<sub>2</sub>O}. Temperature dependent binary parameters are respectively  $\beta_{NaCl}^0$ ,  $\beta_{NaCl}^1$ , and  $C_{NaCl}^{\Phi}$  and  $\beta_{Na,SO_4}^0$ ,  $\beta_{Na_2SO_4}^1$ , and  $C_{Na_2SO_4}^{\Phi}$  in the case of Pitzer's model<sup>3</sup> and  $\tau_{H2O,NaCl}$ ,  $\tau_{NaCl,H2O}$ ,  $\tau_{H2O,Na_2SO_4}$ , and  $\tau_{Na_2SO_4,H2O}$  in the case of Chen's model.<sup>5</sup> Ternary parameters of both models are temperature dependent and must be fitted on data relative to ternary system {NaCl + Na<sub>2</sub>SO<sub>4</sub> + H<sub>2</sub>O}:  $\theta_{Cl^-,SO_4}^{2-}$  and  $\psi_{Na^+,Cl^-,SO_4}^{2-}$  for Pitzer's model and  $\tau_{Na_2SO_4,NaCl}$  for Chen's model.

Application of eqs 10 and 11 for the calculation of dissolution enthalpy brings out to expressions containing

 $-1.93467805 \times 10^{3}$ 

Table	4. Pitzer's Mode	el Parameters and	Corresponding Diss	olution Enthalpie	es at Infinite Dilution	ns (273.15 <	<b>T</b> <	373.15
K). Co	efficients for Pa	rameters (Equatio	n 14)					

parameter	а	b	С	d
$\alpha 1_{NaCl}$	2.0 <sup>a</sup>	0	0	0
$\beta_{\rm NaCl}^0$	$7.65 imes10^{-2}\mathrm{a}$	$-4.27875369  imes 10^2$	-1.21435198	0
$\beta_{\text{NaCl}}^1$	$2.664 imes10^{-1}\mathrm{a}$	$3.43262086  imes 10^2$	1.40203591	0
	$1.27 imes10^{-3}\mathrm{a}$	$5.92892282  imes 10^{1}$	$1.65939470 \ 10^{-1}$	0
$\alpha 1_{Na_2SO_4}$	$1.4^{b}$	0	0	0
$\beta_{N_0,SO}^0$	$-1.727 imes10^{-2}\mathrm{a}$	$-2.56047587 imes10^{3}$	$-1.35084958  imes 10^{1}$	$1.82451748  imes 10^{-2}$
$\beta_{\text{Na}_2\text{SO}_4}^{\text{Na}_2\text{SO}_4}$	$7.534 imes10^{-1}\mathrm{a}$	$-1.77370056  imes 10^4$	$-1.03209462  imes 10^2$	$1.53114111  imes 10^{-1}$
$C^{\phi}_{Na SO}$	$1.1745 imes10^{-2}\mathrm{a}$	$6.60777453  imes 10^2$	3.70285811	$-5.31023797 imes10^{-3}$
$\theta_{\mathrm{Cl}^-,\mathrm{SO}_4^{2-}}$	$2.0184 imes10^{-2}$	$3.48727912  imes 10^2$	1.16954282	0
$\Psi_{Na^+,Cl^-,SO_4{}^{2-}}$	$1.4063  imes 10^{-3}$	$-9.51831180  imes 10^{1}$	$-3.34556419  imes 10^{-1}$	0
	Coefficients for Diss	olution Enthalpy at Infinit	te Dilution (J. mol $^{-1}$ ) (Equation 1	3)
species	$\Delta_{ m sol}H^\circ_m$	$_{i,i}(T_0)$	е	f
NaCl	3.897104	$55 \times 10^3$	$-1.17772160  imes 10^{2}$	0

<sup>a</sup> Ref. [3]. <sup>b</sup> Recommended by Holmes et al.<sup>26</sup>

Table 5. Chen's Model Parameters and Corresponding Dissolution Enthalpies at Infinite Dilutions (273.15  $\leq$  T  $\leq$  373.15 K). Coefficients for Parameters (eq 14)

 $-9.99070349 \times 10^{2}$ 

parameter	а	b	С	d			
$\tau_{\rm NaCl.H_{2}O}$	-4.551ª	$8.18477803  imes 10^2$	2.79814877	0			
$\tau_{\rm H_{2}O, NaCl}$	8.898 <sup>a</sup>	$-2.6537277 imes 10^2$	-1.96527693	0			
$\tau_{\rm Na_2SO_4,H_2O}$	$-3.863^{a}$	$-1.4800427  imes 10^4$	$-8.9658312  imes 10^{1}$	$1.38606364  imes 10^{-1}$			
$\tau_{\mathrm{H_2O,Na_2SO_4}}$	7.934 <sup>a</sup>	$4.11894735  imes 10^4$	$2.40738326 \ 10^2$	$-3.60128428  imes 10^{-1}$			
$\tau_{\rm NaCl,Na_2SO_4}$	1.43211775	$-2.4582335  imes 10^3$	-7.20015676	0			
$\tau_{\rm Na_2SO_4, NaCl}$	$-5.06891535  imes 10^{-1}$	$-2.4534473  imes 10^{-1}$	-6.70352531	0			
Coefficients for Dissolution Enthalpy at Infinite Dilution (J·mol <sup>-1</sup> ; eq 13)							
species	$\Delta_{\mathrm{sol}} H^{\circ}_{m,i}(\mathcal{I})$	T <sub>0</sub> )	е	f			

species	$\Delta_{\rm sol}H_{m,i}(I_0)$	e	I
NaCl Na2SO4	$\begin{array}{c} 3.82018410 \times 10^3 \\ -2.40952023 \times 10^3 \end{array}$	$\begin{array}{c} -1.16626473 \times 10^2 \\ -1.04303949 \times 10^3 \end{array}$	0 1.212529844

<sup>a</sup> Reference 24.

 $Na_2SO_4$ 

also the temperature derivatives of each temperaturedependent parameter.

In previous works,<sup>18,19</sup> the temperature dependence of binary Pitzer's parameters  $\beta_{ca}^0$ ,  $\beta_{ca}^1$ , and  $C_{ca}^{\Phi}$  has been fitted on molar dissolution enthalpy data considering that  $\Delta_{sol}H_{m,r}^{\circ}T^2(\partial\beta_{ca}^0/\partial T)$ ,  $T^2(\partial\beta_{ca}^1/\partial T)$ , and  $T^2(\partial C_{ca}^{\Phi}/\partial T)$  as adjustable parameters at each temperature. Then, by integration, the temperature dependence was obtained. Similar procedure was recently adapted in the case of Chen's model (Marliacy et al.<sup>7</sup>) for determining variation of  $\Delta_{sol}H_{m,r}^{\circ}$ ,  $\tau_{ca,w}$  and  $\tau_{w,ca}$  with temperature.

The same methodology was used in this present work to fit the expression of ternary parameters in the case of both models. First  $T^2(\partial \theta_{\text{CI}^-,\text{SO}4}^{2-}/\partial T)$  and  $T^2(\partial \psi_{\text{Na}^+,\text{CI}^-,\text{SO}4}^{2-}/\partial T)$  in the case of Pitzer's model and  $T^2(\partial \tau_{\text{NaCL},\text{Na}_2\text{SO}_4}/\partial T)$  and  $T^2$ - $(\partial \tau_{\text{Na}_2\text{SO}_4\text{Na}\text{CI}}/\partial T)$  in the case of Chen's model were adjusted at each temperature on our experimental molal dissolution enthalpies reported in the Table 2. Then, the expression of each ternary parameter with respect to temperature could be obtained by integration.

Finally, each parameter and molar dissolution enthalpy at infinite dilution can be represented by

$$\Delta_{\text{sol}} H_{m,i}^{\circ} = \Delta_{\text{sol}} H_{m,i}^{\circ}(T_0) + e(T - T_0) + f(T^2 - T_0^2) \quad (13)$$

parameter = 
$$a + b\left(\frac{1}{T} - \frac{1}{T_0}\right) + c \ln\left(\frac{1}{T_0}\right) + d(T - T_0)$$
(14)

in which  $T_0$  is the reference temperature (298.15 K) and "parameter" is respectively binary and ternary parameters

of Pitzer's and Chen's models. Coefficient "a" is the value of "parameter" at T<sub>0</sub> and coefficients b, c, d, e, f, and  $\Delta_{sol}H_{m,i}^{\infty}(T_0)$  were determined by fitting enthalpy measurements as explained above. In the case of binary parameters, coefficient "a" was taken from literature<sup>3,5</sup> and b, c, d, e, f, and  $\Delta_{sol}H^{\circ}_{m,i}(T_0)$  were fitted on the {NaCl +  $H_2O$  data reported by Hubert et al.<sup>19</sup> and on {Na<sub>2</sub>SO<sub>4</sub> + H<sub>2</sub>O} data reported by Marliacy and co-workers.<sup>7</sup> In the case of ternary parameters, b, c, and d were determined on our experimental dissolution enthalpies in {NaCl + Na2- $SO_4 + H_2O$  and the value at  $T_0$  could be determined by fitting experimental solubility data at  $T_0$  in the ternary system (see Marliacy et al.<sup>20</sup>). The values of the coefficients are reported in Table 4 (Pitzer's model) and in Table 5 (Chen's model). Equations 13 and 14 used in this work are simpler than the complex and empirical functions proposed by the authors. However, their application is limited between (298 and 363) K.

1.12610282

**Representation of the Thermodynamic Properties of** {**NaCl** + **Na**<sub>2</sub>**SO**<sub>4</sub> + **H**<sub>2</sub>**O**}. As shown in Figures 2–4, experimental values of molal dissolution enthalpies are better represented by Pitzer's model than by Chen's model, particularly for systems rich in NaCl (Figure 2). Thus, we have obtained a relative mean deviation of 3.9% with Pitzer and of 6.8% with NRTL-electrolytes. It is interesting to test the influence of temperature dependence in ternary parameters for the calculation of dissolution enthalpy (Figure 5) assuming that ternary parameters are constant with temperature. It is evident that Pitzer's model allows a rather good estimation of data in the 10/1 ternary system; with this model, it seems not necessary to consider a



**Figure 5.** Molal dissolution enthalpy  $(J \cdot kg^{-1})$  of {NaCl (1) + Na<sub>2</sub>-SO<sub>4</sub> (2)} mixtures in water ( $m_1/m_2 = 10/1$ ); comparison with models of Pitzer and Chen in which ternary parameters are assumed to be constant.



**Figure 6.** Activity of water  $a_w$  in {NaCl + Na<sub>2</sub>SO<sub>4</sub> + H<sub>2</sub>O+} system at 323.15 K: $\mathbf{v}$ , NaCl ref 18;  $\Box$ , 1/1 ternary, this work;  $\times$ , 1/10 ternary, this work;  $\mathbf{0}$ , Na<sub>2</sub>SO<sub>4</sub> ref 25; comparison between experimental data and values calculated with Pitzer's model.

temperature dependence for ternary parameters. At the opposite, the Chen's model cannot represent experimental values with a sufficient accuracy with constant ternary parameters.

We have also compared values of activities of water presented in Table 1 with those calculated using Pitzer's and Chen's model. Mean relative deviations are low (0.14% with Pitzer and 0.19% with NRTL-electrolytes). Figure 6 presents experimental data interpolated at 323.15 K using Appelblatt's relation (eq 2) and their representations with Pitzer's model in binary and ternary systems. Activity of water in the ternary is located between activity in {NaCl +  $H_2O$ } and in {Na<sub>2</sub>SO<sub>4</sub> +  $H_2O$ }. It can be pointed that experimental values in the 1/10 ternary system and in the {NaCl +  $H_2O$ } are nearly the same at the same ionic strength.

Pitzer and electrolyte-NRTL have been used to calculate activity coefficients of electrolytes and osmotic coefficients in the ternary system. The performances of two models are compared in Table 6 in which mean relative deviations between calculated values and experimental ones taken from literature are reported. Results obtained with Pitzer

Table 6. Deviations between Experimental andCalculated Values of Activity Coefficients and OsmoticCoefficients in {NaCl + Na2SO4 + H2O} System

				-		
<i>T</i> /K	I/mol⋅kg <sup>-1</sup>	data	Nb. points	Pitzer(%)	NRTL(%)	ref
298.15	1.0	$\gamma_{Na_2SO_4}$	10	2.9	4.7	12
298.15	6.47 - 8.16	$\phi$	5	1.1	3.9	10
278.15	0.375 - 4.8	γNaCl	9	0.4	2.7	8
288.15	0.12 - 4.8	γNaCl	17	0.6	2.1	8
293.15	0.12 - 3.39	γNaCl	8	0.5	1.5	8
298.15	0.12 - 4.8	γNaCl	17	0.4	2.0	8
308.15	0.12 - 4.8	γNaCl	17	0.4	2.0	8
318.15	0.375 - 4.8	γNaCl	9	0.4	2.6	8

are satisfactorily excepting in the case of Synott et al.<sup>12</sup> data. It is evident that electrolyte-NRTL represents the data with a less good accuracy.

#### 4. Conclusions

It was shown that our existing nonisothermal static device described previously<sup>1</sup> was able to measure vapor pressure in the ternary system {NaCl  $(1) + Na_2SO_4 (2) +$ H<sub>2</sub>O(3)} between (298 and 363) K with different molality ratios  $m_1/m_2$ . As in binary systems, experimental values were fitted using Appelblatt's relation<sup>2</sup> (Table 1). That proves the possible of an extension of this apparatus to aqueous electrolyte systems that are more complex than binaries. Dissolution enthalpy measurements of {NaCl (1)  $+ Na_2SO_4(2)$  system in water were also made for different value of  $m_1/m_2$  at 297.8 K, 317.5 K, and 332.4 K. These experimental data (Table 2) were used to determine the temperature dependence of the electrolyte-NRTL and Pitzer model's ternary parameters. As previously shown,<sup>7,18,19</sup> binary parameters of both models could be fitted on dissolution enthalpy values measured in binary systems {salt + water}. Thus, it seems reasonable to claim that this method could be successfully used to fit parameters of numerous thermodynamic models in the case of complex aqueous electrolyte systems. Its main limitation concerns species that are poorly soluble in water, in this case solidliquid equilibrium data must be preferred to determine the variation of the adjustable parameters with temperature. The resulting electrolyte-NRTL and Pitzer's parameters (Tables 4 and 5) lead to the simultaneous representation of our experimental values (Figures 2, 3, 4, and 6) and of some data taken from literature like osmotic coefficient and activity coefficient of both NaCl and Na<sub>2</sub>SO<sub>4</sub> (Table 6). However, Pitzer's model is more capable of representing thermodynamic properties than electrolyte-NRTL. Particularly, the temperature dependence of ternary parameters of Pitzer's model was not necessary to calculate dissolution enthalpies with a good accuracy (Figure 5). In fact, the main advantage of Chen's model is its possible extension to mixed aqueous-organic solutions.

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